



American Computer Science League

2019-2020

Contest #1

INTERMEDIATE DIVISION SOLUTIONS

1. Computer Number Systems

$$2019_{10} = 3743_8$$

Written in ascending octal digits: 3347_8

$$3347_8 = 11\ 011\ 100\ 111_8$$

$$= 110\ 1110\ 0111_{16}$$

$$= 6\ E\ 7_{16}$$

1. $6E7_{16}$ or $6E7$

2. Computer Number Systems

Convert each to binary:

$$\text{a) } 4765_8 = 100111110101_2 \quad 8\ 1's$$

$$\text{b) } ABE_{16} = 101010111110_2 \quad 8\ 1's$$

$$\text{c) } 8271_{10} = 10000001001111_2 \quad 6\ 1's$$

$$\text{d) } 1011111011_2 \quad 8\ 1's$$

2. 8271_{10} or 8271

3. Recursive Functions

$$f(-5) = f(-5 + 3) - 2 = f(-2) - 2 = 0 - 2 = -2$$

$$f(-2) = f(-2 + 3) - 2 = f(1) - 2 = 2 - 2 = 0$$

$$f(1) = f(1 + 3) - 2 = f(4) - 2 = 4 - 2 = 2$$

$$f(4) = f(2*4-1) + 1 = f(7) + 1 = 3 + 1 = 4$$

$$f(7) = 7 - 4 = 3$$

$$f(0) = f(0 + 3) - 2 = f(3) - 2 = 6 - 2 = 4$$

$$f(3) = f(3 + 3) - 2 = f(6) - 2 = 8 - 2 = 6$$

$$f(6) = f(2*6 - 1) + 1 = f(11) + 1 = 7 + 1 = 8$$

$$f(11) = 11 - 4 = 7$$

$$\text{So } f(f(f(f(-5)))) = f(f(f(-2)))$$

$$= f(f(0))$$

$$= f(4)$$

$$= 4$$

3. 4



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4. Recursive Functions

$$f(1) = 3$$

$$f(2) = 5$$

$$f(3) = 3 * f(2) - f(1) = 3 * 5 - 3 = 12$$

$$f(4) = 3 * f(3) - f(2) = 3 * 12 - 5 = 31$$

$$f(5) = 3 * f(4) - f(3) = 3 * 31 - 12 = 81$$

$$f(6) = 3 * f(5) - f(4) = 3 * 81 - 31 = 212 > 200$$

4. 6

5. What Does This Program Do?

5. 32

a	b	c	d	e	f
20	4	10	2		
20	4	10	2		24
20	14	10	2		24
20	14	10	2	14	24
20	24	10	2	14	24
20	4	10	2	14	24
4	4	10	2	14	24

$$\begin{aligned}x &= (f / (a + d) - f / (b * d) + (e + d) / (a * b))^{(f - e) / d} \\&= (24 / (4 + 2) - 24 / (4 * 2) + (14 + 2) / (4 * 4))^{(24 - 14) / 2} \\&= (24 / 6 - 24 / 8 + 16 / 16)^{(10 / 2)} \\&= (4 - 3 + 1)^5 \\&= 2^5 = 32\end{aligned}$$